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### Makale Başlığı / Title

Birim şekil değiştirme enerji yoğunluğunun kaynaklı birleştirmelerin yorulmasına karşı tasarımlardaki uygulamalarının güncel incelemesi

State of the art review of the application of strain energy density in design against fatigue of welded joints

### Yazarlar / Authors

Özler KARAKAŞ<sup>1\*</sup>, Nail TÜZÜN<sup>2</sup>

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# Birim İyileştirme Yöntemleri ile Birlikte Strain Enerji Yoğunluğu Kullanılarak Yapılan Bir İnceleme

## State of the art review of the application of strain energy density in design against fatigue of welded joints

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İletişim: okarakas@pau.edu.tr, naituzun@gmail.com

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- İletişim: okarakas@pau.edu.tr

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### Öz

Mechanical components against fatigue is vitally important to prevent sudden and unexpected damage. Due to the complex nature of welded joints because of the changes in material properties due to heat and the geometry of weld beads, designing against fatigue becomes an even more challenging task. Over the years, various methods have been developed to determine fatigue parameters. In this paper, a state of the art literature review of studies based on strain energy density (SED) approach is presented. While the background is provided, the main focus of the paper is to evaluate the applications of SED approaches. In order to achieve this, papers with varied topics that related to SED are evaluated.

Anahtar kelimeler: Strain energy density, fatigue behaviour, welded joints

### Abstract

Design of mechanical components against fatigue is vitally important to prevent sudden and unexpected damage. Due to the complex nature of welded joints because of the changes in material properties due to heat and the geometry of weld beads, designing against fatigue becomes an even more challenging task. Over the years, various methods have been developed to determine fatigue parameters. In this paper, a state of the art literature review of studies based on strain energy density (SED) approach is presented. While the background is provided, the main focus of the paper is to evaluate the applications of SED approaches. In order to achieve this, papers with varied topics that related to SED are evaluated.

Keywords: fatigue behaviour, strain energy density, fracture mechanics, welded joints

## 1 Introduction

Fatigue, as widely known, is a phenomenon observed on mechanical components under cyclic loading. Due to the sudden and unexpected nature of fatigue failures, the determination of fatigue related parameters is crucial in any engineering design.

The importance of fatigue is no exception for welded joints which are widely used in many engineering components and constructions. But it must be stated that the complexity of welds and heat related changes in welded material properties, make accurate determination of fatigue parameters a challenging task. Therefore, modern methods for evaluating the fatigue of welds are continuously developed and improved.

Local strain energy density (SED) approach is one of such modern methods, currently used in evaluation of fatigue.

While the idea of using strain energy as a material parameter is not new, developments in computer aided analyses and calculations provided the method the necessary increase in mathematical accuracy and ease of use, increasing its use in fatigue estimations. Proposed by Lazzarin et al. [1,2], SED approaches are derived from the calculation of strain energy in a designated control volume near notch tip to determine an energy parameter to estimate the initiation of fatigue failure.

## 2 Theoretical basis and Applications of SED Approaches

Elastic and plastic deformations occur during cyclic loading. This causes dissipation of heat and an increase in internal potential energy. The increase in this strain related potential energy continues until a state of equilibrium is reached or fatigue damage occurs. Thus, the amount of strain energy at which fatigue damage occurs can be considered a damage parameter.

By considering the strain energy per unit volume, a strain energy density parameter can be calculated (SED). SED can be determined as a damage parameter that encompasses the both phases of fatigue damage which are crack initiation and propagation. A generalized equation for calculating the total SED is presented in [1,2];

$$(1)$$

where  $SED$  is total stress components and  $\epsilon$  is total strain components.

Originally developed for sharp V notches, the simplified equation serves as a basis for the local SED approaches. Methods, which will be discussed in this paper, modifying the original approach are further developed over time to cover different stress states, loading components and notches.

2.1 Sharp V notch SED approach

sharp V notch is in question, instead of maximum stresses at the tip of the notch, a stress value averaged over a finite length is considered. Elaborating on this idea, Lazzarin and Zambardi [1,2] proposed that SED values around the tip of a sharp V notch can be averaged over a finite volume with a radius of R. The finite volume question is named critical volume and presented in Fig. 1. The averaged SED value is considered to be material parameter for static or cyclic crack initiation.

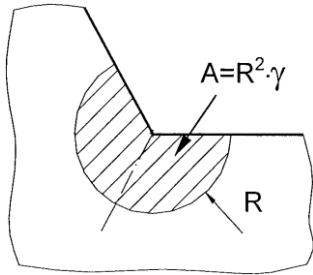


Figure1: Critical volume surrounding the notch tip [1].

The area A(R) of critical volume is represented in Eq. 2 as following;

$$(2)$$

where is the internal notch angle based on the notch opening angle . Both notch angles are schematically represented in Fig. 2.

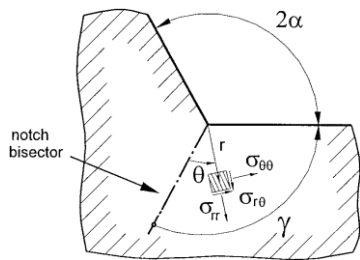


Figure2: Notch angles in polar coordinate system for notch tip [1].

By averaging the strain energy over A(R) area, Eq. 3 representing the average local SED acquired.

$$(3)$$

where is the strain energy, and are total strain energy coefficients, and are the Notch Stress Intensity Factors (NSIF), and s are the Notch Stress Intensity Factors (NSIF), and s are the Notch Stress Intensity Factors (NSIF). All stress distributions are denominated with scripts 1 and 2 respectively. Total strain energy coefficient and can be expressed as functions of notch opening angle. This relation is presented in Fig. 3 and total strain energy coefficients is plotted against the notch opening angle

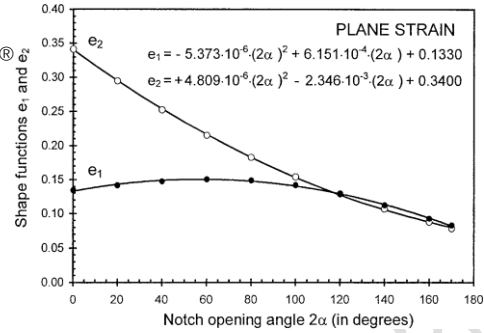


Figure3: Plot of total strain energy coefficients against the notch opening angle [1].

As stated in [1], specimens under loads will fail when average local SED in the control volume reaches a critical SED value. In other words, a relation exists between these SED values. can be determined according to Eq. 4

$$(4)$$

where is the ultimate strength and is a material parameter, independent from the loading type and the notch opening angle. Since the radius of area of the critical volume is also considered to be a material parameter, average local SED can be considered independent from the geometry.

Based on these conclusions, value is considered to be applicable to fatigue assessments. However, instead of the calculation of , average local SED range is taken into consideration [4].

Results of analytical energy based approaches were compared to experimental data by various scientists over the years. In this article more recent studies on the topic of the application of energy based approaches are evaluated.

Expanding on the previous findings, Lazzarin et al. [5], presented a discussion regarding the relation between SED and notch stress intensity factors using some welded joints and plates with sharp notches. Assessed fatigue data was previously evaluated in [6], in relation to the averaged SED and was expanded with the addition of more experimental results. Average SED plotted against number of cycles (W are presented in Fig. 4. Highly stressed regions of notches were evaluated via the use of the critical volume which was used to average SED. By presenting a relation between SED and NSIF, determining the NSIF values were simplified. This approach was determined to fit for purpose of fatigue strength evaluation of welded joints and calculation of theoretical stress concentration factors for blunt shaped and V shaped notches and holes

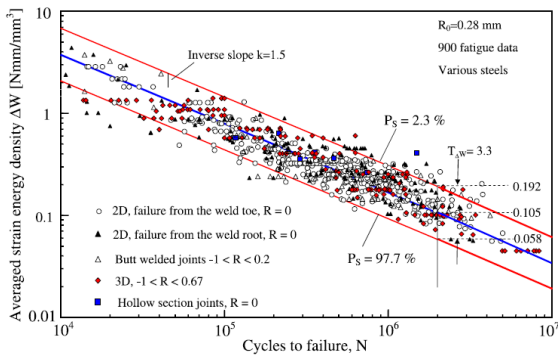


Figure 4: Fatigue strength of welds as a function of the averaged local SED [5].

## 2.2 Applications of SED approaches

By considering a different approach Payten et al. [7], proposed a model which takes the energy dissipated in the material on a macroscopic level as a parameter of the creep fatigue damage occurred in the material, expanding the use of strain energy in fracture mechanics. The method considered both stress and temperature data in fatigue assessments. Estimations made by the proposed energy density exhaustion method were compared with the creep fatigue test results of low alloy ferritic steels and showed good agreement with the experimental creep fatigue lives.

Park et al. [8] assessed the fatigue life behaviour of rolled AZ31 based on the low cycle fatigue tests performed along the rolling direction. In the study, instead of average SED, a total strain energy based model was used, incorporating plastic SED as a fatigue parameter to approximate the fatigue life of the specimens. While stress and strain based fatigue assessment approaches were difficult to use due to the characteristics of the material, the experimental results and the estimations made by the model based on total strain energy showed good correlation (Fig. 5). The study was further expanded in [9] to evaluate the anisotropic fatigue behaviour of rolled Mg-Al-Zn alloy comparing the fatigue of normal direction and rolling direction to the rolling plane. An energy based approach which took the mean stress effect into consideration was used to evaluate the anisotropic fatigue life behaviour of the specimens.

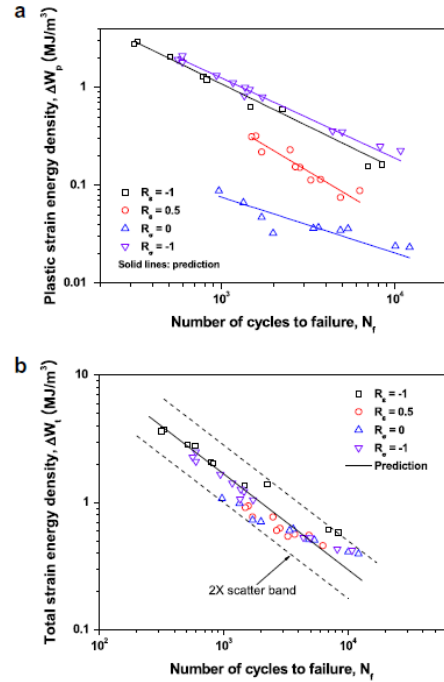


Figure 5: Fatigue life estimations based on (a) plastic SED, and (b) total SED [8].

By considering the working conditions of gas turbine engines, a multiaxial fatigue assessment was considered in [10]. In order to determine the fatigue life of specimens under shear or biaxial bending loads Scott and Quakpor et al. presented a method based on rain energy. Energy based shear and multi-axial fatigue life estimation criteria were proposed. The methods were used to evaluate the fatigue test results from three different aluminium alloy specimens. Energy based methods successfully managed to estimate the fatigue life of specimens. Further improving on the subject, a new hysteresis loop representation was presented in [11], to improve the accuracy of fatigue life estimations performed using SED. Experiments were carried out on Al 6061 specimens and SED per cycle was observed and a new representation of the hysteresis loop was developed based on the significant changes in the SED during failure cycles.

Further study based on these works was presented by Ozaltun et al. [12]. Based on hysteresis energy, a new fatigue life estimation framework was developed. The new framework was intended to perform fatigue life estimations for service gas turbine materials, taking the aging effects caused by cyclic loadings into consideration to calculate the remaining life of the turbine. The method was validated by comparison between results of calculations using the model and fatigue test results of Al 6061 showing good agreement between two results.

Kim et al. [13], investigated the strain influence on the low cycle and high cycle fatigue behaviour of BCC Mn twinning induced plasticity steel. A modified energy based approach was used to determine the effects of pre-strain and mean stress on the fatigue life and was developed to successfully establish a correlation between low cycle and high cycle fatigue data. The method also proved to be successful in fatigue life estimations of cyclically non-stabilized materials.

In order to develop an efficient total fatigue life computation method, Maksimovic et al. incorporated cyclic deformation properties obtained from low cycle fatigue with a fatigue crack growth model based on SED concept [14]. Fatigue tests were conducted on flat specimens with central hole made of quenched and tempered high alloy high temperature steel 13H11N2V2MF. Estimations made using the computation model were in agreement with the experimental results as can be observed in Fig. 6.

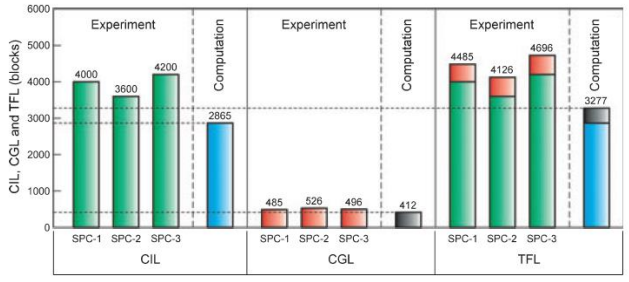


Figure 6: Comparison of experimental and computational results of crack initial, crack growth life and total fatigue life [14].

Based on the approach developed by Lazzarin et al., Mehran et al. assessed the applicability of averaged SED criteria to estimate the critical fracture load in notched plates functionally graded materials [15]. Experimental results on functionally graded austenitic martensitic steel specimens with blunt notches under mode I loading were evaluated using J integral and averaged SED criteria. Both criteria were applicable in estimating the critical fracture load in specimens. While the averaged SED was established as a criterion for fatigue estimation for homogenous materials, this study proved that the approach can also be applied to non-homogenous materials.

In order to present an accurate low cycle fatigue life estimation for gas turbine components, a probabilistic method with an energy based damage parameter was developed by Zhu et al. [16]. The framework was devised to include the uncertainty of various fatigue damage parameters as required and is presented in Fig. 7. Included damage parameters were Smith-Topper (SWT), plastic strain energy density (PSED), FSC criterion (FSC), thermodynamic entropy (TE), costy-based damage parameter (VDP) and generalized damage parameter (GDP).

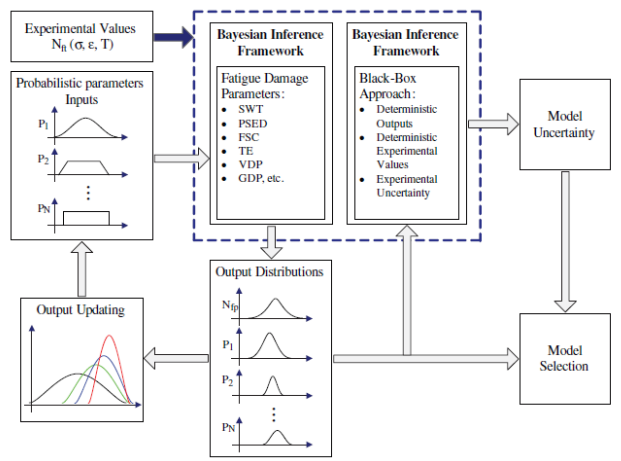


Figure 7: Probabilistic low cycle fatigue life estimation. In the study, the model uncertainty for the generalized damage parameter, Smith-Topper and plastic SED were quantified by measuring the differences between model estimations and experimental data. Experimental data were acquired from specimens made of GH4133 tested at various temperatures. In [17], the research further expanded with a new model to also consider the fatigue damage. A plastic SED based fatigue damage parameter was developed. The proposed model estimated the fatigue behaviour of GH4133 compared plastic SED approach and Smith-Topper with relative success, determining that plastic SED approach is inadequate to account for the creep fatigue damage on its own.

Walat et al. presented a criteria based on strain and energy determine the low cycle fatigue life and multiaxial stress state [18]. The criterion in question can be represented as Eq. 5 in its most basic form. However, reading the original publication is highly recommended to understand the use and the development of the criteria.

$$(5)$$

Where  $\sigma_t$  is the tangent component of the energy parameter on the critical plane since the energy criteria previously used in high cycle range and performed accurately in low cycle range, as shown in this study, it can be said that the proposed criteria is universal and can be applied to both high and low cycle fatigue.

While mainly an experimental study, Shariati et al. [19], presented interesting results by performing stress controlled uniaxial fatigue tests on Polyoxymethylene (POM). Based on the experimental results, the strain range, strain ratcheting, SED and the slope of the stress-strain hysteresis loops were determined. The stress, strain and energy approaches were used to calibrate material constants. The stress and energy approaches were determined to be relatively better for the fatigue life estimations of POM compared to strain approaches.

In [20], Lazzarin et al. investigated the fracture behaviour of isotropic graphite specimens with inclined keyhole notches using the previous developments in SED as basis. A local energy criterion was used for the fracture prediction, enabling presentation of experimental data in a unified scatter band regardless of the notch geometry and mode mixity. Mode mixity was evaluated based on Eq. 6. The proposed criterion accurately estimated the critical loads of the specimens.

$$-\dot{\sigma} \otimes \epsilon^o - \dot{\sigma}^a \quad (6)$$

In order to more accurately study the behaviour of cyclic fractures, Boulenouar et al. [21], developed a numerical propagation model under mixed mode loading conditions. In order to calculate the stress intensity factors under mode I and mixed mode loading, finite element code was modified with displacement extrapolation method. The SED approach was mainly used to improve the code to estimate the new course of crack propagation.

In [22] criterion based on the averaged SED proposed by Lazzarin et al. was compared with Leguillon's criteria from the Finite Fracture Mechanics theory.

acquired from the experimental studies literature was used to compare each criterion and a good agreement was found in all cases. SED and Carpinteri approaches generally showed conservative results compared to approach based on averaged SED for V-shaped and blunt V-shaped notches under torsion in [23]. The expressions were applied to experimental data. The data consisted of torsion tests performed on cracked, notched and smooth specimens. The analytical expressions was validated by a number of finite element analyses and shown agreement with the results.

Based on the local average SED approach and NSIF, Ferro [24] provided numerical simulation analyses of residual stress distribution near notch tip caused by cyclic loading. A model based on the local strain energy was proposed to determine the fatigue resistance of stressed components. The method required calculation of the asymptotic residual stress field in term of NSIF accurately.

In order to extend the use of SED for fatigue estimations at elevated temperatures, Berto et al. investigated the stress controlled fatigue test results of CuBe alloy specimens at temperatures up to 650 °C in [25]. Two different specimen geometries were used for the uniaxial tension experiments which were hourglass shaped and plates with a central hole. SED approach was successfully used to compile all fatigue data in a single scatter band regardless of the geometry specimens

Further expanding the wide range of applications of SED approaches, Torabi et al. presented experimental, theoretical and numerical study on brittle fracture of notched Polymethylmethacrylate (PMMA) specimens in [26]. Fracture tests under mode II loading were performed on Brazilian disk (Fig. 8) type specimens which have V-notches with end holes. Fracture loads were estimated using averaged SED criterion and showed good correlation with the experimental results.

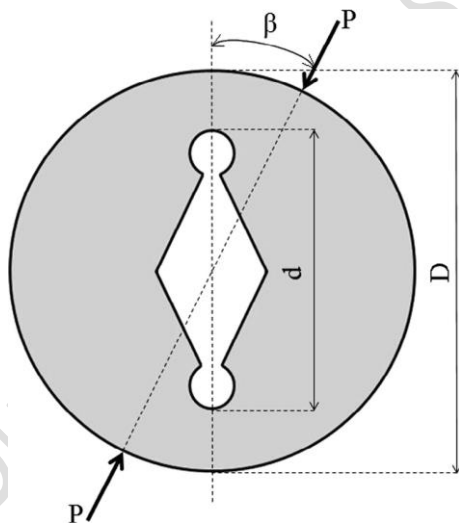


Figure 8: Brazilian disk specimen which has V-notches with end holes [26].

By considering fatigue test results of C45 carbon steel 718, and directionally solidified superalloy 717 specimens tested at temperatures of 250° C, 500° C, and 850° C respectively Gallo et al. [27], evaluated the accuracy of average SED approach when evaluating the fatigue data of notched components at elevated temperatures. Average SED

approach was able to compile the fatigue data to a single narrow scatter band regardless of the component geometry.

Wang et al. proposed a modified SED exhaustion model in order to estimate creep fatigue life under tension hold only [28]. The model took mean stress and stress relaxation into consideration as well. Experiments performed on specimens made of Grade 91 steel, Alloy 617 and 304 stainless steel were evaluated using the proposed model. According to these estimations, most of the test results were in an acceptable range within a scatter band. The proposed model resulted in more accurate estimations compared to previously used methods for creep fatigue life calculations.

Chandran et al. proposed a new, more direct approach based on the net section strain energy rate to determine the growth rates of fatigue crack [29]. The approach used the change in net section strain energy amplitude with crack extension unlike methods based on range of stress intensity factor. The proposed approach relatively simplified the calculation of crack growth rate of mini-specimens of Ti-6Al-4V alloy

in [30], Zhu et al. proposed a model for estimation of fatigue life of metals based on mean stress corrected strain energy. The dissipated strain energy was modified by two mean stress correction factors and mean stress corrected total SED was derived as presented in Eq. 7.

$$(7)$$

where  $\sigma_f$  is fatigue strength coefficient,  $n_f$  is fatigue ductility exponent,  $K$  is material constant. 13 different experimental datasets were evaluated using the proposed model and comparisons with generalized damage parameter, Morrow Smith Watson Topper and Walker were made. Proposed model managed to achieve more accurate estimation

Further improving SED approaches, Razavi et al. performed extensive brittle fracture tests on cracked granite samples subjected to various inplane loading mixities in [31]. Also theoretical estimations of fracture loads were made using an approach based on average SED criterion. Experimental data were in good correlation with the theoretical estimations.

In addition to the articles summarized in this paper [31][32] should be considered for further reading for more information on frequently used terms in aforementioned articles, low cycle and high cycle fatigue, mean stress effects and damage parameters.

### 3 Conclusions

As presented by the many articles presented in this study, SED based approaches show promising results in estimating fatigue and fracture related parameters of notched and welded specimens with different loading types and wide variety of different materials. Also, it is possible to use SED approaches in estimations at various temperatures, both high and low. The independency of the approach from the geometry of the specimens is also worth mentioning considering the possibility of complex geometries of welded constructs.

Future research in this field to incorporate SED based approaches in fatigue and fracture related estimations can be

fruitful in determining the full capabilities of energy based methods. By determining energy based material parameters for different materials, fatigue related calculations can be performed with less effort. Thus, fatigue studies based on strain energy should be encouraged to contribute to establishing a standard for fatigue related energy parameter.

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